

Experiment - 1

Write a program to define a function executes from command prompt, which shows convergence or not convergence of sequence $f(n) = f_n = \{[3 + 2\sqrt{n+1}]/(\sqrt{n+1})\}$ to 2.

ii) Graph of the sequence $f(n) = (3 + 2 * \text{sqrt}(n+1))/\text{sqrt}(n+1)$
function seqvar (1, N)

```
i = 1;
n = 1 : N;
function f = fun1(n)
```

```
f = (3 + 2 * sqrt(n+1)) / sqrt(n+1)
end function
```

```
if i <= n & abs(fun1(i) - 1) > abs(fun1(i+1) - 1)
    i = i + 1;
else
```

```
    disp("sequence is not convergent")
end
```

```
xtitle("Graph of the sequence  $f(n) = (3 + 2 * \text{sqrt}(n+1))/\text{sqrt}(n+1)$ ")
```

```
Plot(n, fun1)
```

```
Plot(n, fun1=1, "r--")
```

```
P = gca();
```

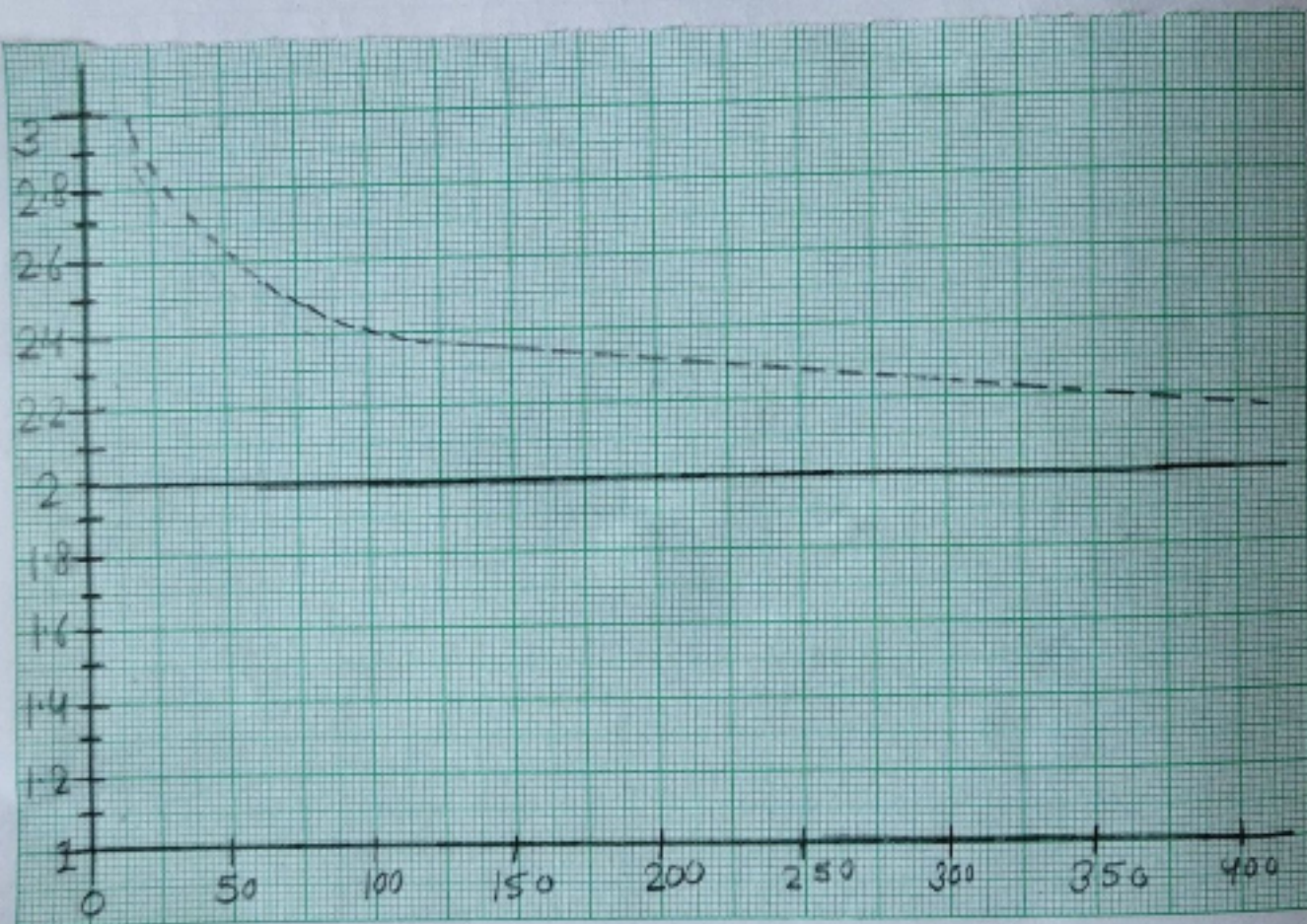
```
P.data_bounds = [1, 1 - 1; N, 1 + 1];
```

Signature

Exponential

*Graph of Exponential function
y = a * b^x
where a is the initial value
and b is the growth factor.*

*If b > 1, the function is increasing.
If 0 < b < 1, the function is decreasing.*



```
gcf() - axes_size = [700 500];  
endfunction
```

Execute and Input

```
--> exec ('/users/co11egeadmin/sequen.sce',-1)  
--> seq_var (2,400)
```

Observation Ex-4 :

From the graph of the function sequence $f(n) = f_n = \{ [3 + 2\sqrt{n+1}] / \sqrt{n+1} \}$ we have observed that the graph is going to the two ($l=2$) line as n is increasing. Therefore we can say that this sequence is convergent or converging to 2.

Experiment - 2

Write a program for sequence $\langle (-1)^n/n \rangle$ which is bounded by $[-1, 1]$. Then verify Bolzano Weierstrass Theorem that this sequence has at least one limit point. If it has two limit point then show graphically that there are two subsequences converging on the points.

// "Graph of the sequence $f(n) = (-1)^n/n$ "
format (3);

function seq_bdd (a, b, N)

$i = 1$;

$n = 1 : N$;

function $f =$ fun2 (n)

$f = (-1)^n/n$

endfunction

if $i \leq n$ & $\text{abs}(\text{fun2}(i) - a) > \text{abs}(\text{fun2}(i+1) - a)$
 $\text{abs}(\text{fun2}(i) - b) > \text{abs}(\text{fun2}(i+1) - b)$

$i = i + 1$;

$\text{disp}(\text{"limit point of the sequence is / are"})$
 $\text{disp}(\text{fun2}(10000));$

```

disp (fun2 (10001));
if abs (fun2 (10000) - fun2 (10001)) < .00001
disp ("sequence is convergent and converging to"
      fun2 (10000));

```

```

else

```

```

disp ("sequence is oscillatory consisting two
limit points. So it has subsequences converging
on these limit points");

```

```

disp ("First limit point is", fun2 (10000));

```

```

disp ("second limit point is", fun2 (10001));

```

```

end

```

```

else

```

```

disp ("sequence is not convergent")

```

```

end

```

```

xtitle ("Graph of the sequence  $f(n) = (-1)^{n/n}$ ")

```

```

plot (n, fun2, ".")

```

```

plot (n, fun2 (1000), "r-")

```

```

plot (n, fun2 (10001), "r-")

```

```

p = gca();

```

```

p.data_bounds = [1, a; N, b];

```

```

gcf().axes_size = [700 500];

```

```

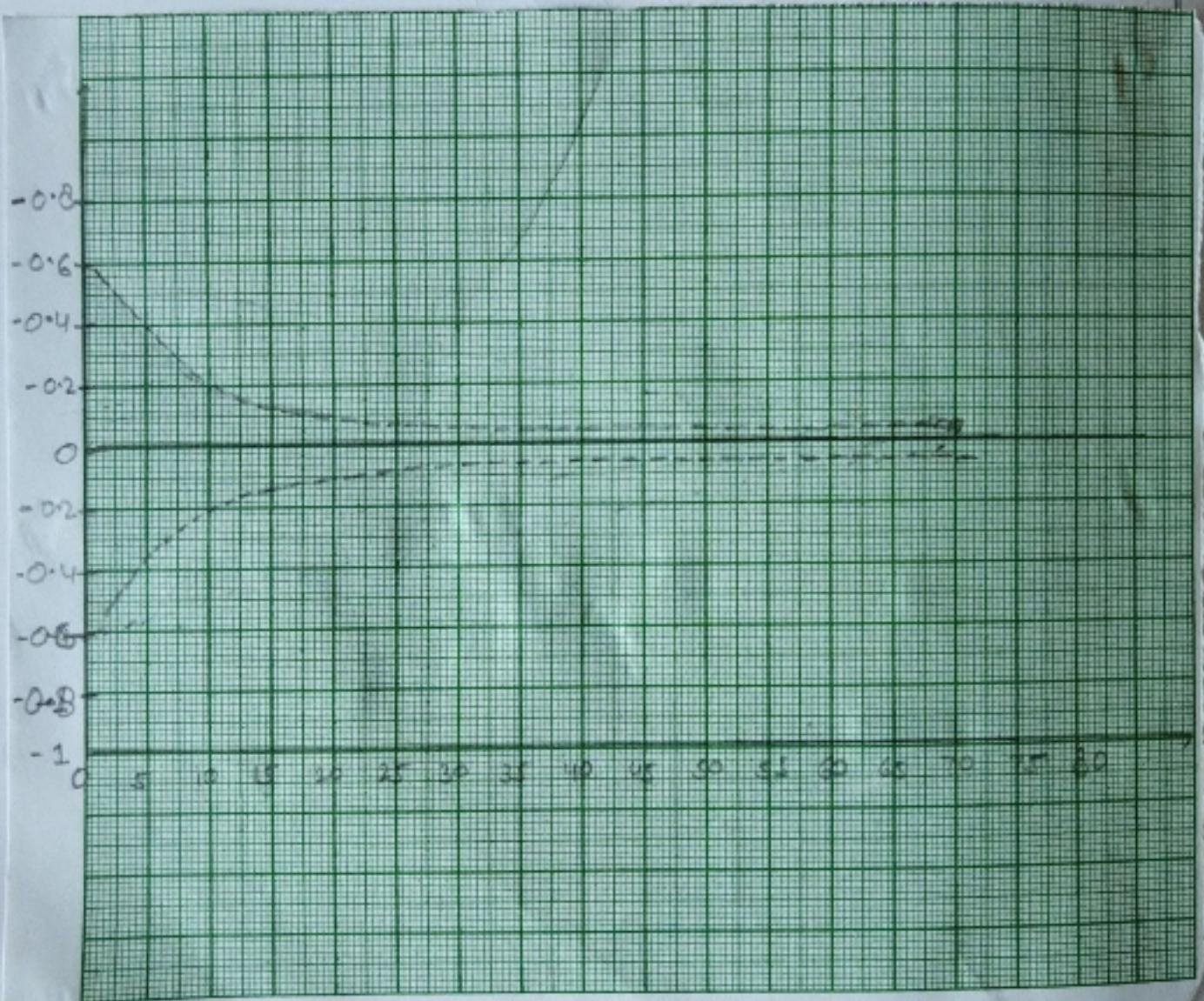
end function

```

Serial No.

Notes

Date



signature

Input function variable value

--> seq = bdd (-1, 1, 1000)

Output :

"Limit point of the sequence is /are"

0.00001 // about to 0

-0.0000010 // about to 0

"Sequence is convergent and converging to"

0.00001 or zero

Observation Ex-2 :

From the output graph we can say that this sequence $\langle (-1)^n / n \rangle$ converging to 0 (zero) although its all subsequence converge to zero yet two subsequence $(1/n \& -1/n)$ but both sequence have different graph which shows the convergence to zero.

Experiment - 3

Write a program to draw a surface of revolution of the curve $y^2 = 4ax$ about y -axis.

// Revolution of the parabola $y^2 = 4ax$
about y -axis
 $a = 2$;

$u_1 = \text{inspace}(-8, 8, 150)$;

$v_1 = \text{inspace}(-\%pi, \%pi, 150)$;

def (" [x, y, z] = fun(u, v)", ["x = ((u^2)/(4*a)) * cos(v)", "y = u",
"z = ((u^2)/(4*a)) * sin(v)"];

orig = [0 0 0];

[xx, yy, zz] = eval13(fun, u1, v1);

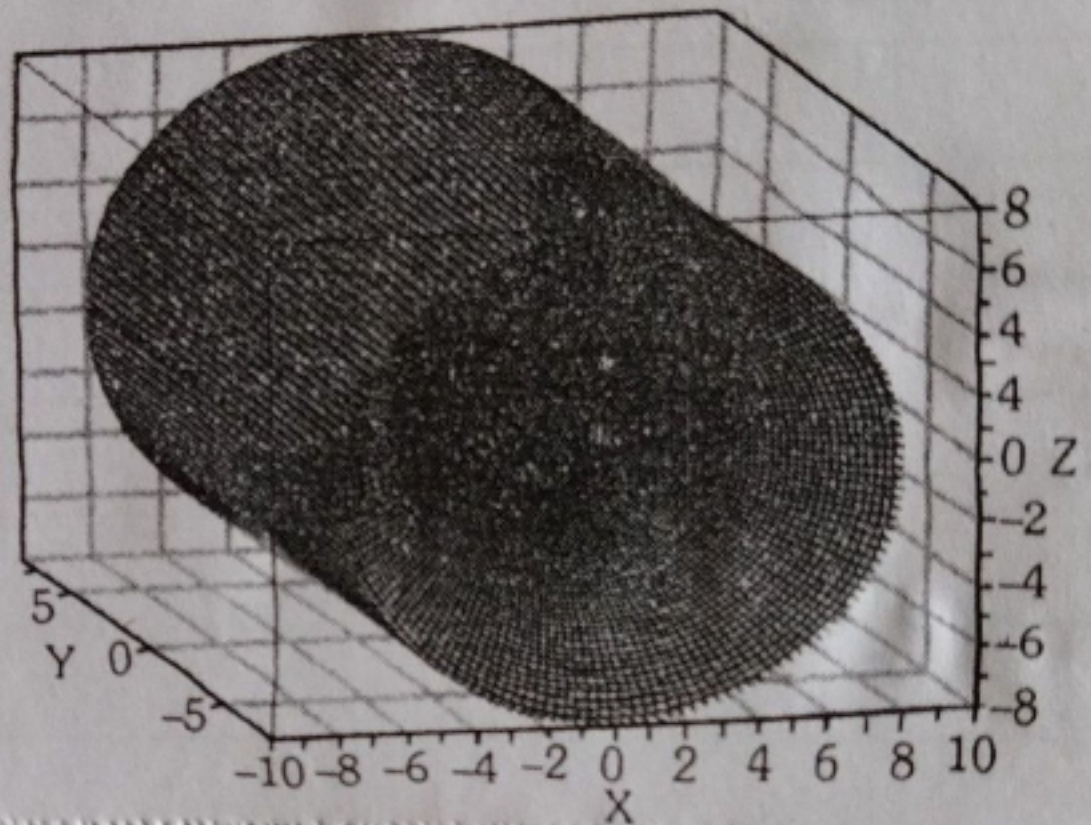
clf ();

surf (xx, yy, zz);

axis (5, 3, 1)

OUTPUT:

The surface generated by the revolution of the parabola $y^2 = 4ax$ about Y-axis for $a=2$



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Notes

Date

07-12-2023

xtick1 ("The surface generated by the Revolution
of the parabola
 $y^2 = 4ax$ about y -axis for $a=2$ ")

gcf().color_map = coolwarm(50);

$\alpha = gca().$

$\alpha.data_bounds = [-10, -0.8; 10, 0.8]$

$\alpha.rotation_angles = [70, 250];$

Experiment - 4

Write a Program to draw a surface of revolution of the tractrix.

$$x = a \cdot \cos(t) + \frac{1}{2} \cdot a \cdot \log(\tan^2(t/2)),$$

$$y = a \cdot \sin(t) \text{ about } x\text{-axis.}$$

// Revolution of the Tractrix

$$x = a \cdot \cos(t) + \frac{1}{2} \cdot a \cdot \log(\tan^2(t/2)),$$

$$y = a \cdot \sin(t)$$

$$a = 3;$$

$$u_1 = \text{ linspace } (-16, 16, 100);$$

$$v_1 = \text{ linspace } (-\%pi, \%pi, 100);$$

$$\text{def } [x, y, z] = \text{fun}(u, v)$$

$$[x = a * \cos(u) + (a/2) * \log(\tan(u/2)^2);$$

$$orig = [0 \ 0 \ 0]$$

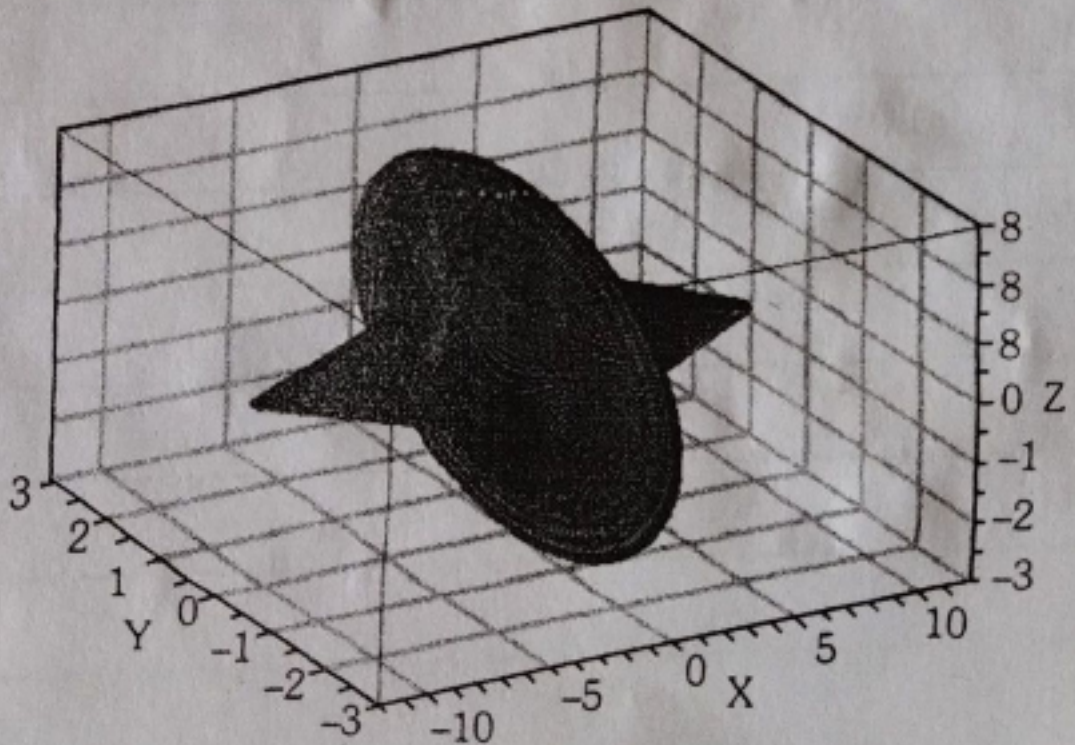
$$[xx, yy, zz] = \text{eval3dp}(\text{fun}, u_1, v_1);$$

$$\text{clf};$$

$$\text{surf}(xx, yy, zz);$$

OUTPUT:

The surface generated by the revolution of the Tractrix $x = a \cos(t) + \frac{1}{2} a \log(\tan^2(t/2))$, $y = a \sin(t)$ about X-axis



Example 8: Write a program to draw a surface of revolution of the Lemniscate $r^2 = a^2 \cdot \cos(2u)$ about the initial line.

`xgrid (5, 3, 1)`

`xtitle ("The surface generated by the
revolution of Trajectory $x = a \cdot \cos(t) +$
 $\frac{1}{2} \cdot a \cdot \log(\tan^2(t/2))$, $y = a \cdot \sin(t)$
about x-axis")`

`a = gca();`

`a.data_bounds = [-12, -3, -3; 12, 3, 3]`

`a.rotation_angles = [55 240];`